



CIKM2017
SINGAPORE

Relaxing Graph Pattern Matching With Explanations

Jia Li¹, Yang Cao², Shuai Ma¹

¹Beihang University, China

²University of Edinburgh, UK



北京航空航天大学
BEIHANG UNIVERSITY



University of Edinburgh

Background



Graph pattern matching

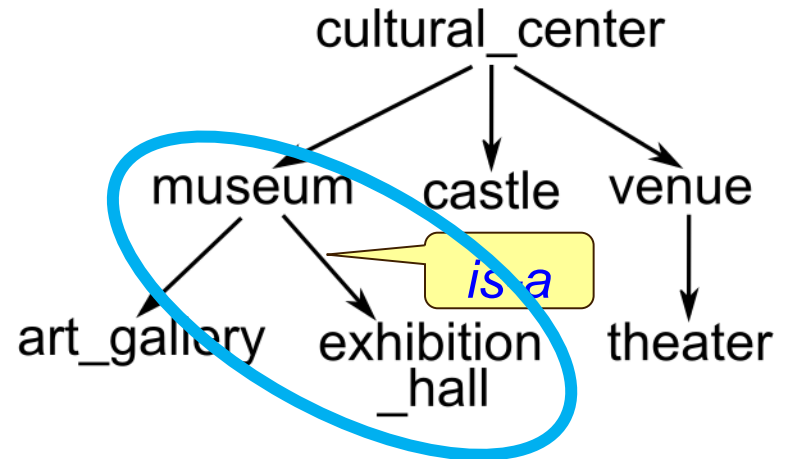
Bijjective function

Subgraph isomorphism

Too Restrictive to find matches

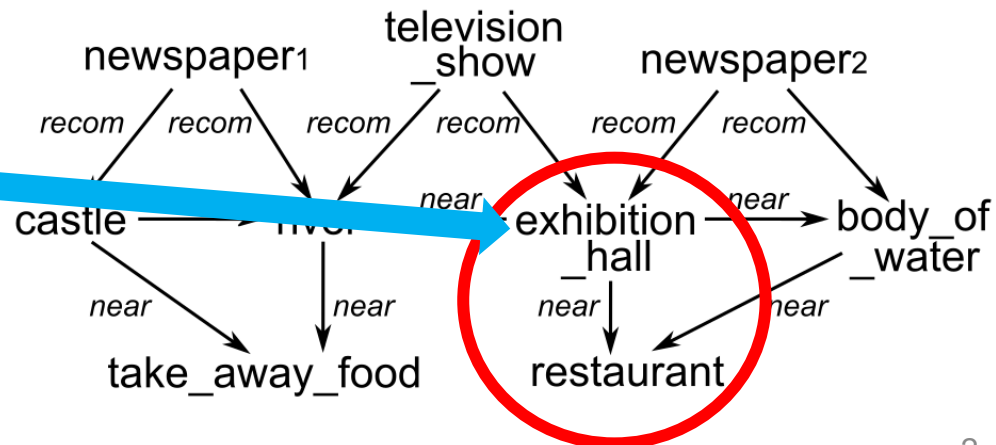
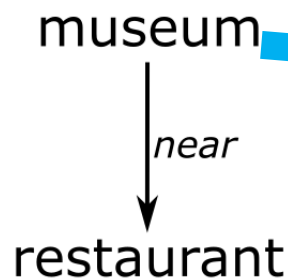
Taxonomy subgraph isomorphism

(Partial) Taxonomy T



Data graph G

Pattern graph Q



Background



Graph pattern matching

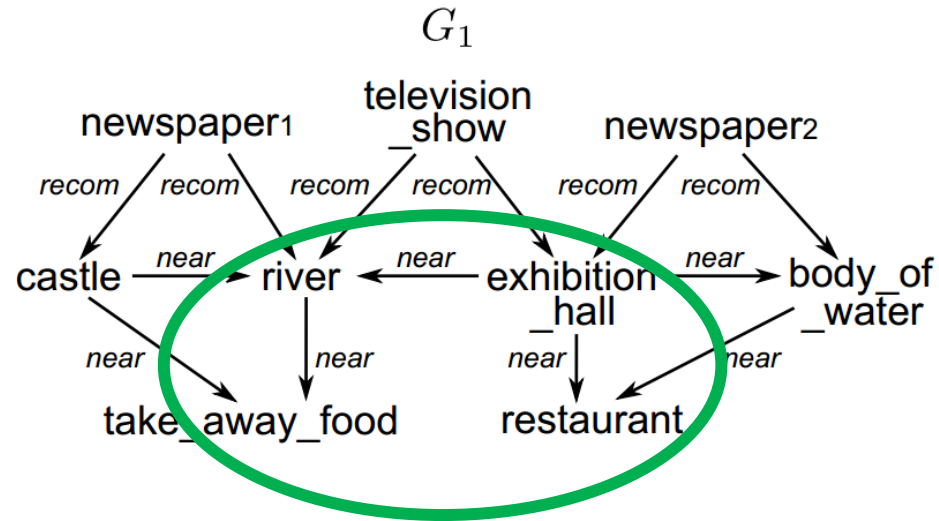
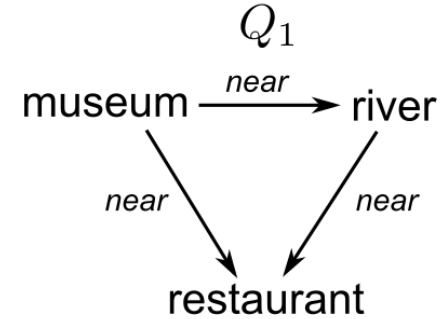
Bijjective function

Subgraph isomorphism

Too Restrictive to find matches

Still too restrictive

Taxonomy subgraph isomorphism



Relax the topological constraints of taxonomy isomorphism



Taxonomy simulation

➤ Taxonomy simulation

Given a data graph $G(V, E, f)$ and a taxonomy $T(V_T, E_T, f_T)$, G matches Q w.r.t. T via taxonomy simulation denoted by $Q \triangleleft G$, if there exists a left-total binary match *relation* $R_T \subseteq V \times V_T$ such that:

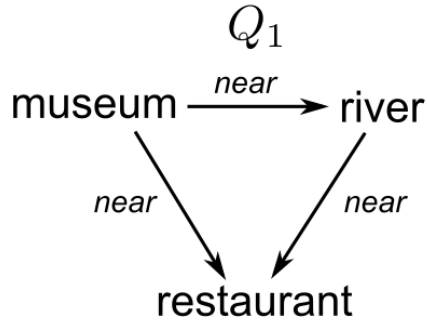
Relation instead of bijective function

Relaxed label matching

- (1) for each $(u, v) \in R_T$, $f(v) \in \text{desc}_T(f_Q(u))$; and
- (2) for each edge $e = (u, u') \in E_Q$, there exists an edge $e' = (v, v') \in E_T$ such that $(u', v') \in R_T$ and $f_Q(e) = f_T(e')$.

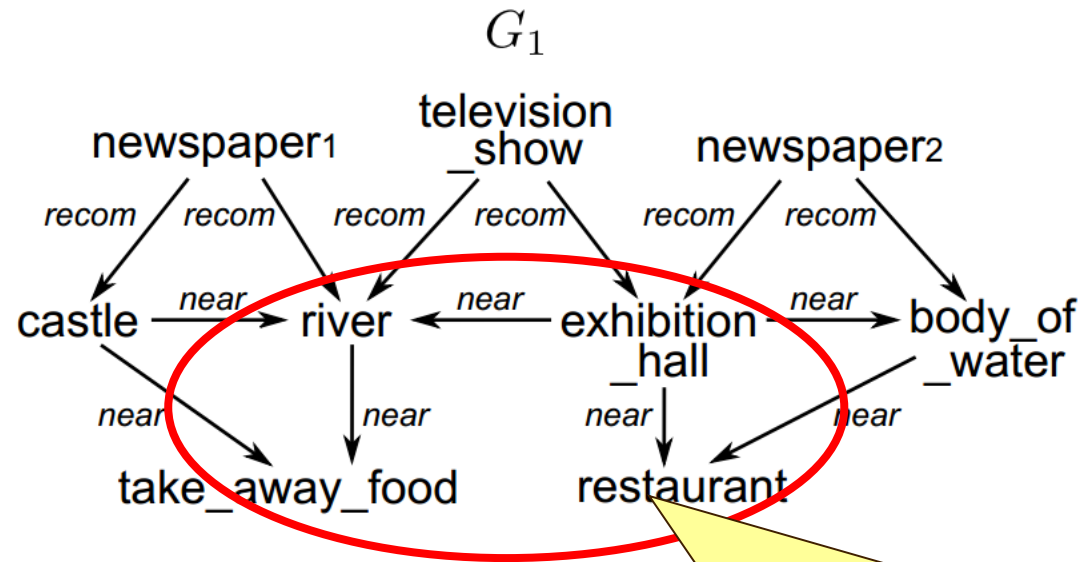


Taxonomy simulation



Match results for Q1 in G1

- museum: exhibition_hall
- river: river
- restaurant: { take_away_food, restaurant }



*Relation-based structural mapping
Taxonomy-based label matching*

It is in $O(|Q||G|)$ time to compute taxonomy simulation

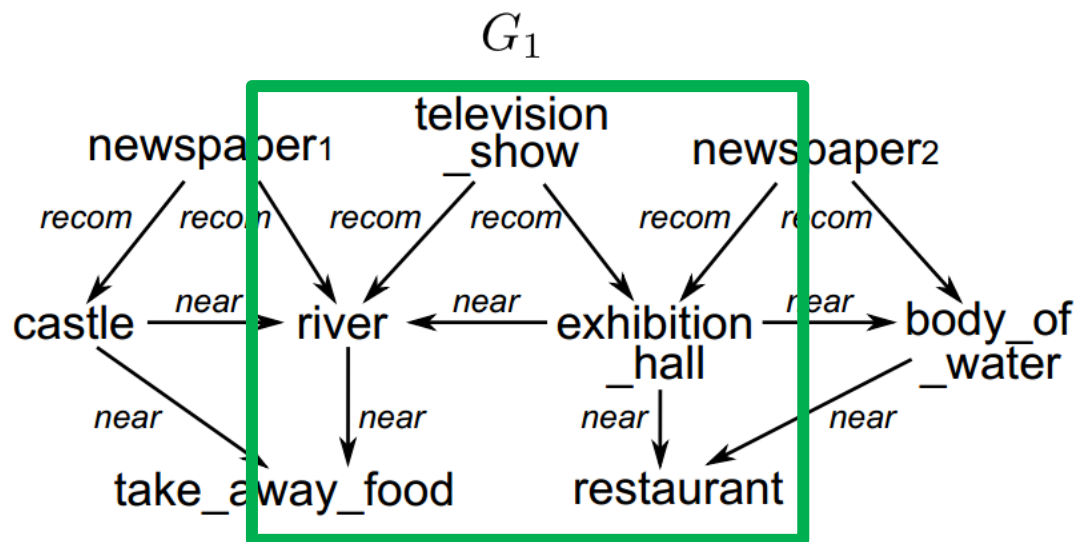
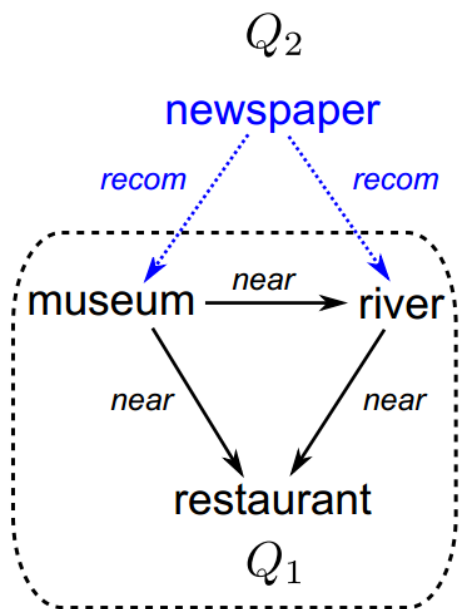
comes with no price w.r.t graph simulation!



Taxonomy simulation

- An experiment (*percentage of patterns with non-empty match results*)

$ V_Q $	2	4	6	8	10
DBpedia	90%	18%	0%	0%	0%
YAGO	54%	2%	0%	0%	0%



We need to further relax taxonomy simulation for larger patterns

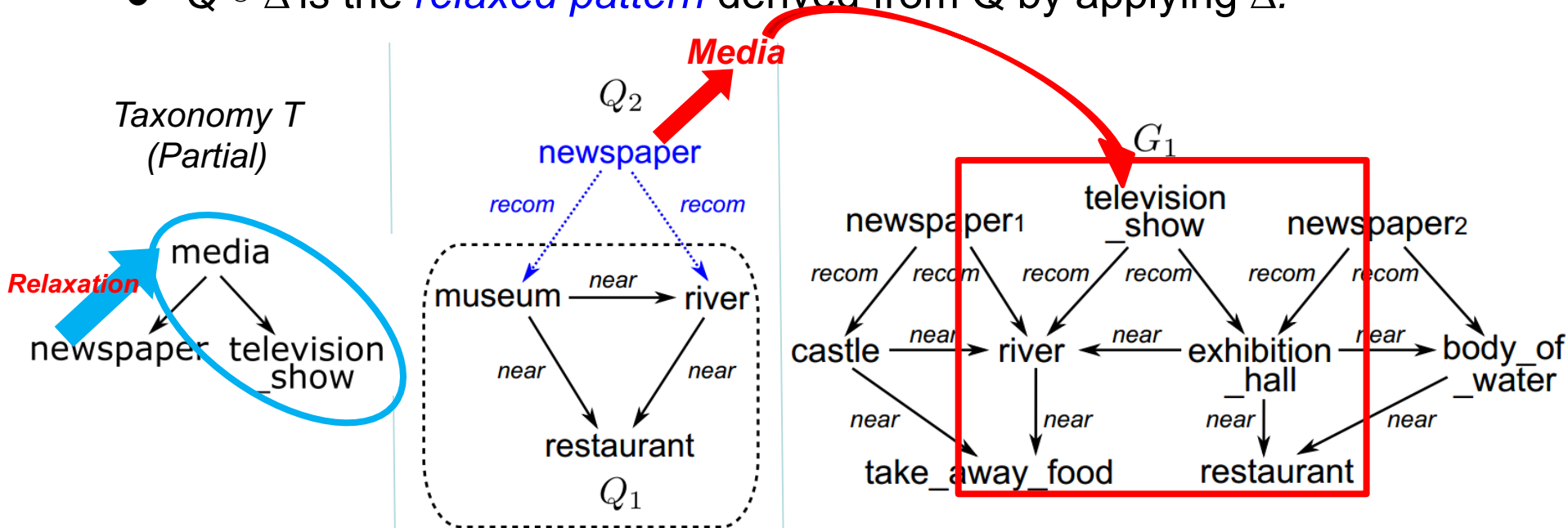
Taxonomy simulation relaxation

➤ Label relaxation

A label relaxation δ w.r.t. a taxonomy T is of form $l \rightarrow l'$ such that l' is an ancestor label of l in T .

➤ Pattern relaxation

- A *pattern relaxation* Δ for Q w.r.t. T is a set of label relaxations for Q .
- $Q \oplus \Delta$ is the *relaxed pattern* derived from Q by applying Δ .



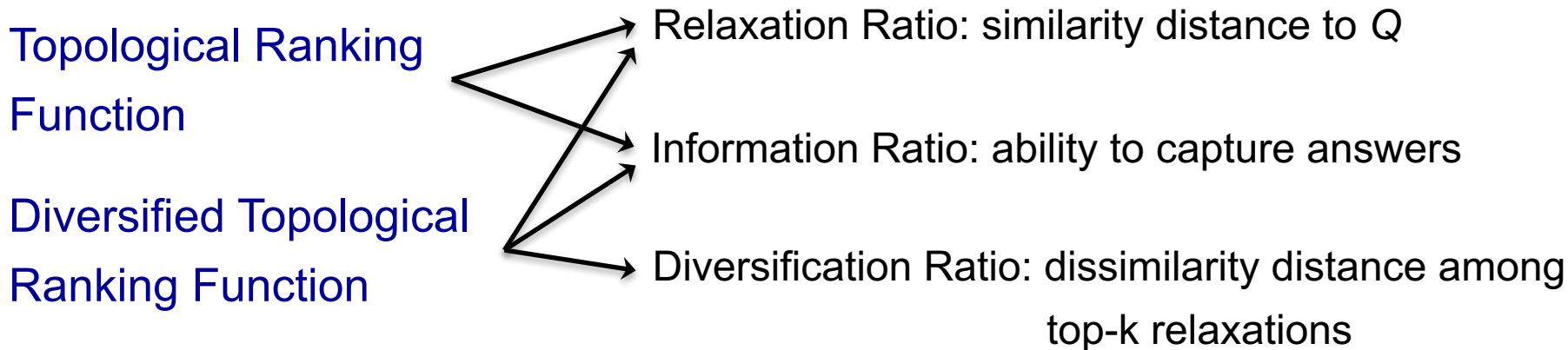


A relaxation framework

- **Ranking top-k relaxations.**
- **Evaluating top-k relaxations.**
- **Relaxation explanation.**



Ranking top-k relaxations



➤ Problems:

- ◆ Top-k pattern relaxation problem (kPR): topological ranking
- ◆ Diversified top-k relaxation problem (kPR_{DF}): diversified topological ranking

➤ Results:

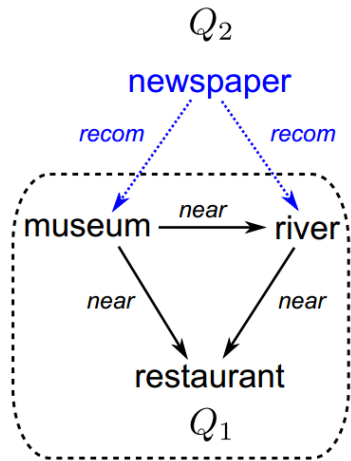
- ◆ kPR problem is in PTIME: in quadratic time, adopt *Lawler's procedure* for computing top-k results
- ◆ kPR_{DF} problem is NP-hard and APX-hard: reduction to well-solved *maximum dispersion problem (maxDP)*



Evaluating top-k relaxations

➤ Problem:

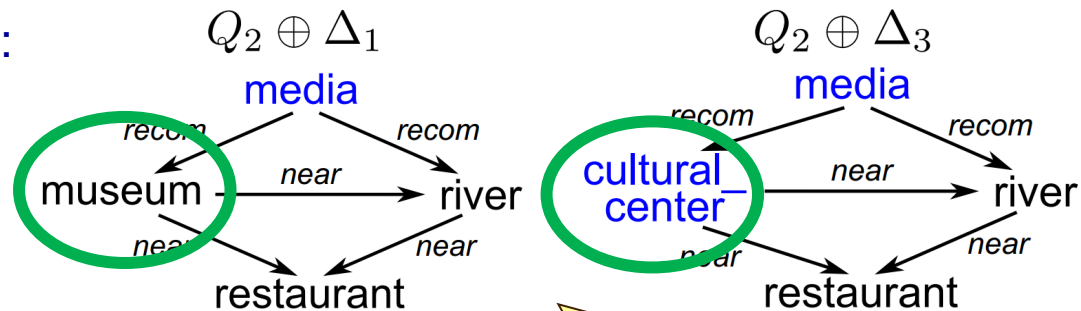
Given Q , G , T and k pattern relaxations $\Delta_1, \dots, \Delta_k$, we aim to compute answers to the relaxed patterns $Q \oplus \Delta_1, \dots, Q \oplus \Delta_k$ in G w.r.t. T .



Pattern relaxations:

$$\Delta_1 = \{ \delta_1 \}$$

$$\Delta_3 = \{ \delta_1, \delta_2 \}$$



Almost the same

Label relaxations:

$\delta_1 = \text{newspaper} \rightarrow \text{media}$

$\delta_2 = \text{museum} \rightarrow \text{cultural_center}$

$\delta_3 = \text{river} \rightarrow \text{natural_place}$

$\delta_4 = \text{river} \rightarrow \text{body_of_water}$

$$Q_2 \oplus \Delta_1(G) \subseteq Q_2 \oplus \Delta_3(G)$$

$Q_2 \oplus \Delta_1(G)$ can be derived from $Q_2 \oplus \Delta_3(G)$ via **bounded decremental taxonomy simulation**

One pass of evaluation to compute both!



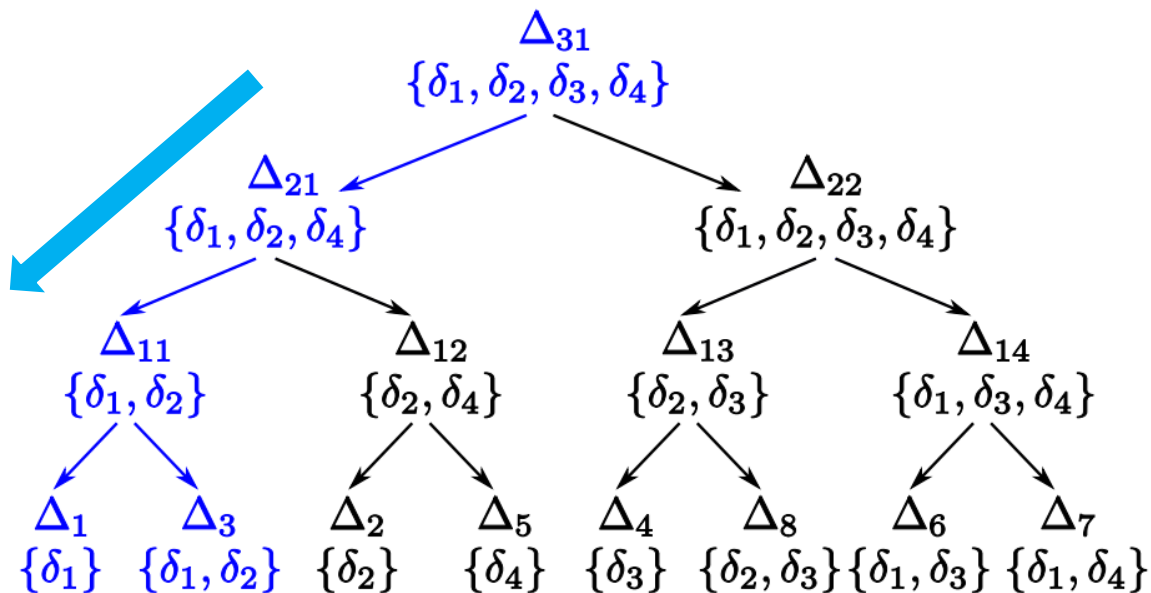
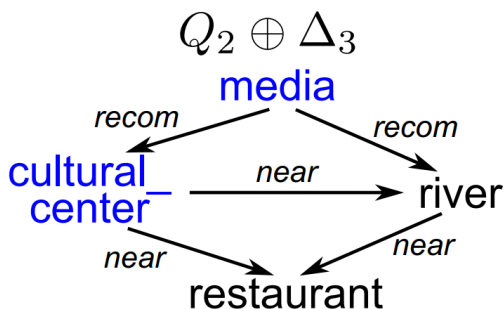
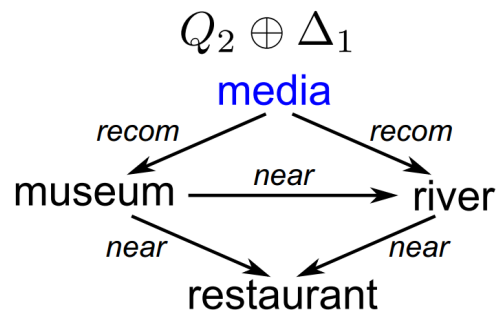
Evaluating top-k relaxations

➤ Problem:

Given Q , G , T and k pattern relaxations $\Delta_1, \dots, \Delta_k$, we aim to compute answers to the relaxed patterns $Q \oplus \Delta_1, \dots, Q \oplus \Delta_k$ in G w.r.t. T .

➤ An algorithm to maximize computation sharing

- ◆ Minimum pairing tree construction
- ◆ Bounded decremental evaluation



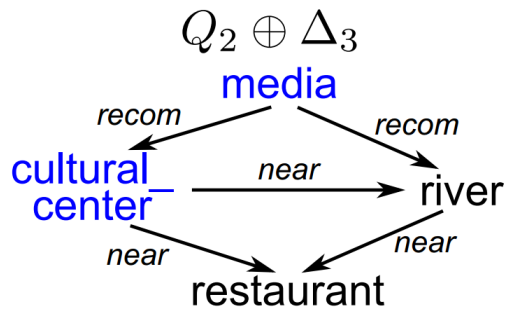


Relaxation Explanation

Can we explain why we return a match by relaxation?

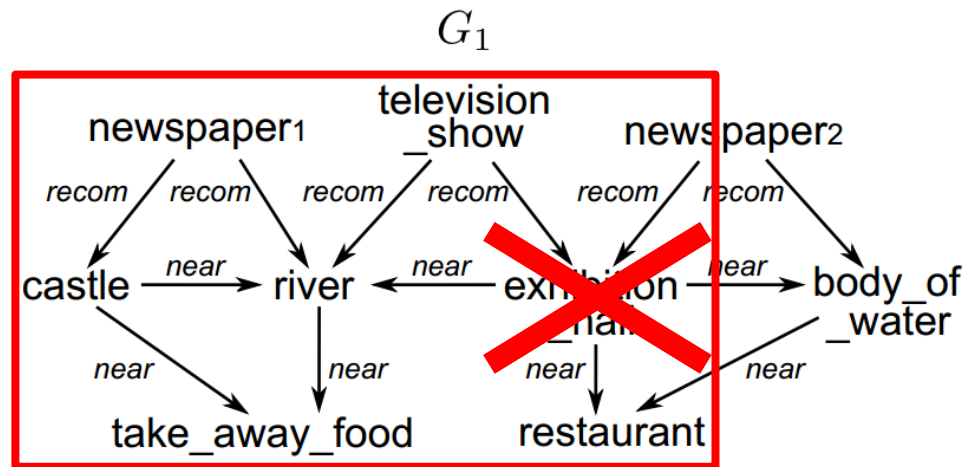
➤ Explanation:

Given data graph G , pattern Q , taxonomy T , pattern relaxation Δ , and a node v in G that is in the match result $(Q \oplus \Delta)(G)$ to the relaxed pattern $Q \oplus \Delta$, an *explanation* for v w.r.t. Δ , denoted by $E\Delta(v)$, is a subset of Δ such that v is in $(Q \oplus E\Delta(v))(G)$.



$$\Delta_3 = \{ \delta_1 = \text{newspaper} \rightarrow \text{media}, \delta_2 = \text{museum} \rightarrow \text{cultural_center} \}$$

$$E\Delta_3(\text{exhibition_hall}) = \{ \delta_1 \}$$





Relaxation Explanation

Can we explain why we return a match by relaxation?

➤ Explanation:

Given data graph G , pattern Q , taxonomy T , pattern relaxation Δ , and a node v in G that is in the match result $(Q \oplus \Delta)(G)$ to the relaxed pattern $Q \oplus \Delta$, *an explanation* for v w.r.t. Δ , denoted by $E\Delta(v)$, is a subset of Δ such that v is in $(Q \oplus E\Delta(v))(G)$.

➤ Problem:

Input: G, Q, T, Δ, v .

Output: **minimum** explanation for v in Δ .

Instances: MRE_{TF} , MRE_{DF}

➤ Results:

- ◆ MRE_{TF} : optimal linear algorithm
- ◆ MRE_{DF} : NP-hard, parameterized algorithm by M



Experimental setting

➤ Real-life graphs:

(1) YAGO:

data graph: (5.13M, 5.39M),

taxonomy graph: a forest with 6488 nodes, average height 3.27 (maximum height 13)

(2) DBpedia:

data graph: (4.43M, 8.43M),

taxonomy graph: a forest with 735 nodes, average height 2.29 (maximum height 6)

➤ Pattern graphs:

implement a generator for producing random pattern graphs $Q(V_Q, E_Q, f_Q)$,

controlled by 3 parameters: $|V_Q|$ varying from 2 to 10, $|E_Q| = \lfloor \alpha |V_Q| \rfloor$, and the number $\lfloor \beta |V_Q| \rfloor$ of labels



Effectiveness of taxonomy simulation and relaxation

➤ Quality

$$\text{acc}(S, Q, G) = \sum_{(u, v) \in S} \text{valid}(u, v) / |S|$$

● *DBpedia*

- ❑ *Taxonomy simulation: 98%*
- ❑ *Relaxations: 77%*

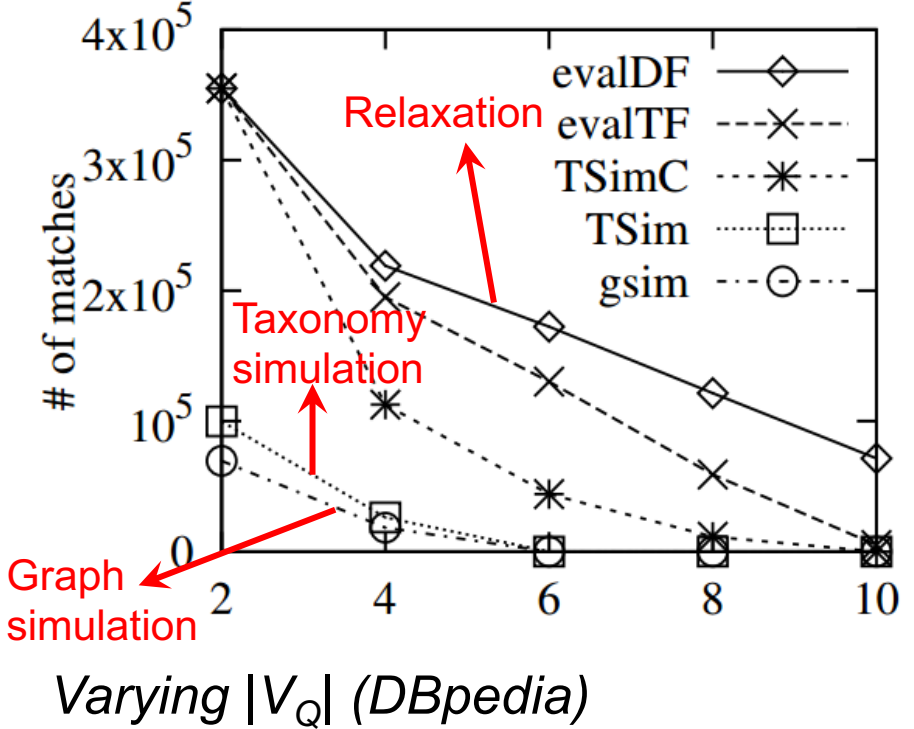
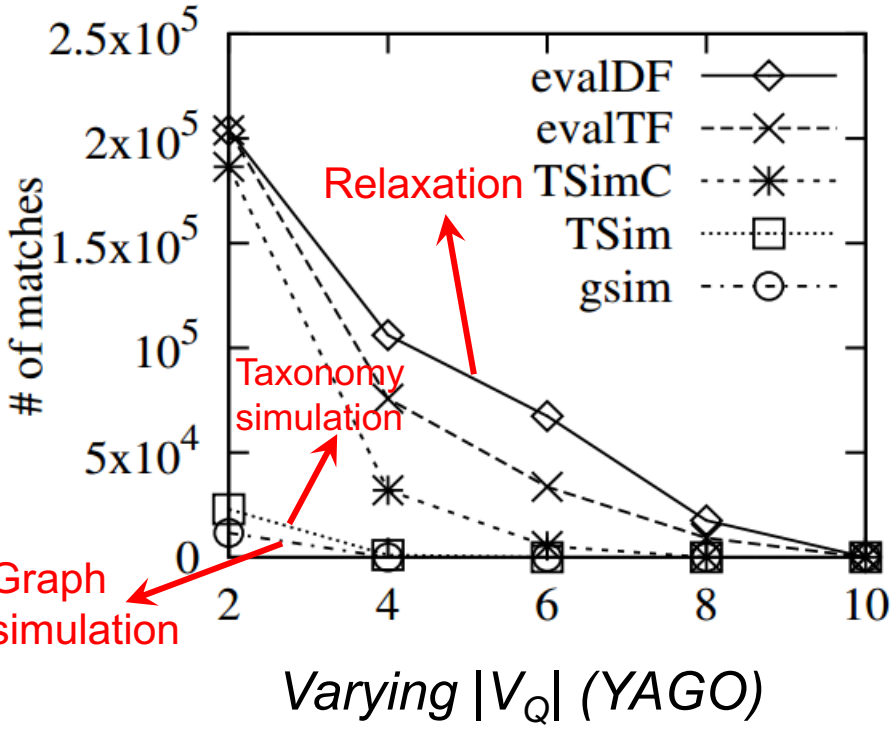
● *YAGO*

- ❑ *Taxonomy simulation: 94%*
- ❑ *Relaxations: 71%*



Effectiveness of taxonomy simulation and relaxation

➤ Quantity (number of matches vs. $|V_Q|$)



Taxonomy simulation vs. graph simulation

- 1,116 vs 0 ($|V_Q|=4$)

Relaxation vs. taxonomy simulation

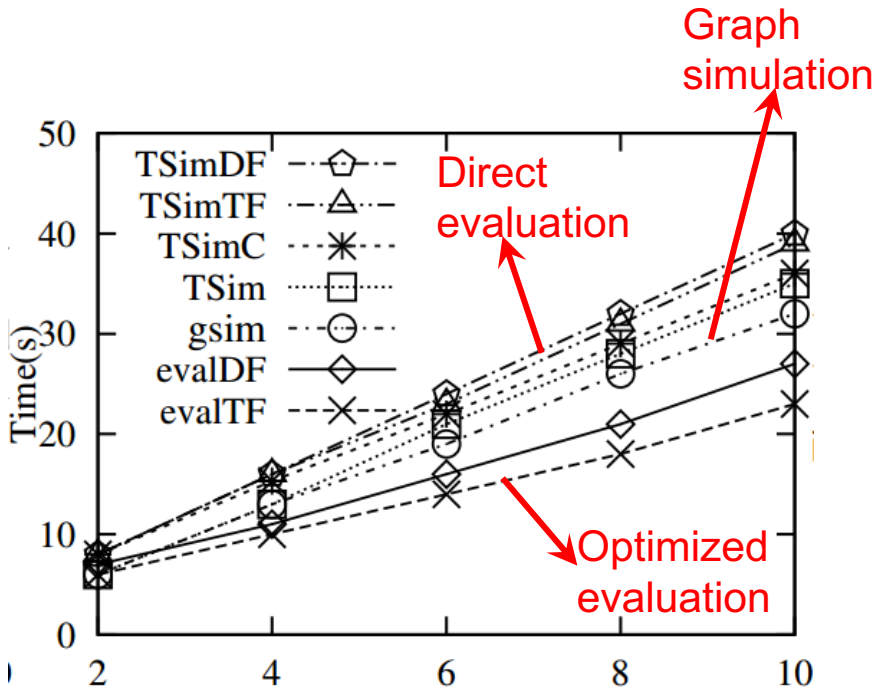
Taxonomy simulation vs. graph simulation

- 26,242 vs 18,384 ($|V_Q|=4$)

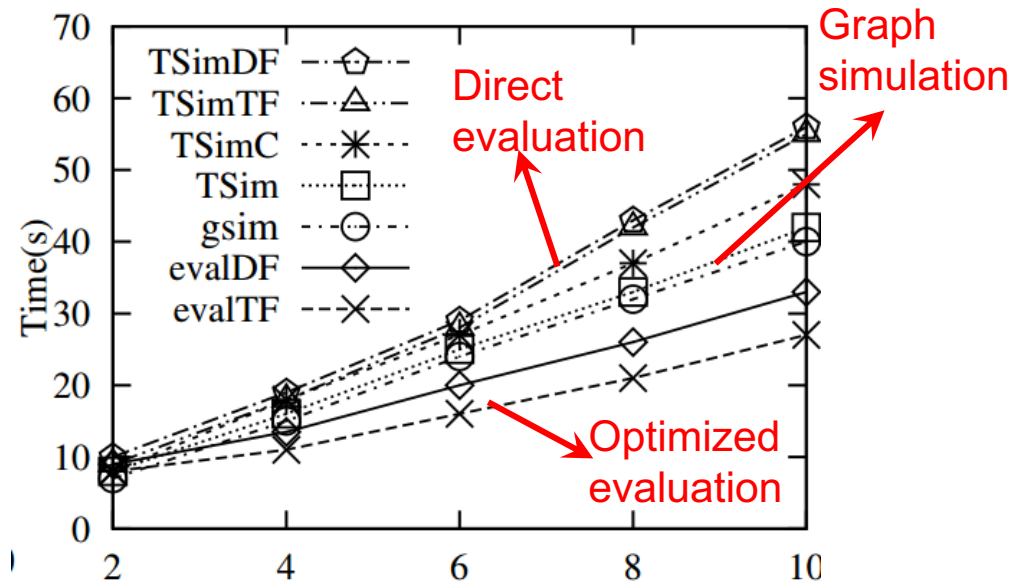
Relaxation vs. taxonomy simulation

$|V_Q| \leq 4$: Taxonomy simulation; $|V_Q| > 4$: Relaxation

Efficiency of relaxation



(d) Varying $|V_Q|$ (YAGO)



(c) Varying $|V_Q|$ (DBpedia)

Direct evaluation / optimized evaluation

- 1.57 times faster ($|V_Q|=6$, YAGO)
- 1.62 times faster ($|V_Q|=6$, DBpedia)



Summary

A framework for relaxing graph pattern matching queries

- Taxonomy simulation by combining taxonomy with graph simulation
- Relaxation framework for taxonomy simulation
 - Ranking functions for taxonomy simulation patterns
 - Computing top-k relaxed patterns
 - Evaluating top-k relaxed patterns
 - Relaxation explanation



Thanks!



Subgraph isomorphism and graph simulation

- ✓ **Subgraph isomorphism:** Graph G matches pattern Q via subgraph isomorphism denoted by $Q \triangleleft G$, if there exists a subgraph G_s of G that is isomorphic to Q . There exists a **bijection** h from V_Q to V_s , such that

NP-hard

(a) edge $(u, u') \in E_Q$ if and only if $(h(u), h(u')) \in E_s$; (b) for each $u \in V_Q$, $l_Q(u) = l(h(u))$.

- ✓ **Graph simulation:** Graph G matches pattern Q via graph simulation, denoted by $Q \prec G$, if there exists a **binary match relation** $R \subseteq V_Q \times V$ such that

Quadratic time

(a) for each $(u, v) \in R$, $l_Q(u) = l(v)$;

(b) for each $u \in V_Q$, there exists $v \in V$, such that (i) $(u, v) \in R$, and (ii) for any edge (u, u') in Q , there exists an edge (v, v') in G such that $(u', v') \in R$.